# TopQuants Newsletter

#### Inside this issue:

V	0	ur	ne	2,	lss	ue

#### March 2014

#### Editorial

#### Dear Reader,

2

4

6

8

9

П

The TopQuants team is pleased to present the first issue of our 2014 newsletter series. We are happy with the positive feedbacks received on our March and September 2013 newsletter issues and the increased number of contributions. We encourage you all to contact us with your ideas and submissions which can include technical articles, blogs, surveys, book/article reviews, opinions (e.g. on newly proposed regulations), coverage of interesting events, research results from Masters/PhD work, job internships etc.

This issue starts with a presentation by De Nederlandsche Bank (DNB), our host for the upcoming TopQuants Spring event in May 2014. Jon Vogelzang (Supervisor, Risk/ALM) and Jantine Koebrugge (Policy Advisor, Financial Risk Management) share their experiences as being part of the team within DNB that is involved in the preparatory work for the European Single Supervisory Mechanism.

Some speakers (Joris van Velsen, Roald Waaijer, Dimphy Hermans, David Schrager, Tony de Graaf, Robert Daniels, Cornelis Oosterlee) from the November 2013 TopQuants Autumn Workshop had enthusiastically responded by providing summaries of their talks and follow up research work which have been included in this issue. The summaries are very much appreciated as they provide a

good recap of the talks and backdrop of this study is the also serve as a brief tutorial proposal by Basel Committee on that topic. on Banking Supervision to

This issue also features five full length articles contributed by people from academia and industry. The first article is by Eric Beutner, Antoon Pelsser and Janina Schweizer from the Maastricht University who update us on their research work in the area of Least Square Monte Carlo (LSMC) method used for pricing complex path dependent options. This is an advancement of their work presented in the first issue of TopQuants newsletter in March 2013.

The next two articles are from Deloitte Financial Consultancy Firm. Florian Reuter and Arjan de Ridder highlight the results and findings from the recently conducted Global Model Practice Survey (GMPS) 2013, a biannual initiative from Deloitte that surveys global model practices within financial institutions. This study emphasizes on the increased use of complex models within banks, the associated model risks involved and the need for effective Model Validation teams within banks to manage model risk. In another Gerdie Knijp and article, Niek Crezée compare the metrics of Value-at-Risk (VaR) and Expected Shortfall (ES) with regard to their robustness to different model or assumption

backdrop of this study is the proposal by Basel Committee on Banking Supervision to adopt ES as a market risk measure as an alternative to the existing VaR measure.

Continuing on regulatory requirements, the Dutch Central Bank (DNB) introduced the Internal Liquidity Adequacy Assessment Process (ILAAP) in the Netherlands beginning June 2011, which is in addition to the liquidity risk management tools within Basel III / CRD IV. Elmo Olieslagers, Bert-lan Nauta and Aron Kalsbeek from Double Effect, present a working paper on Risk/ALM that recommends the Dutch ILAAP as a liquidity risk management tool for Europe and a potential tool to mitigate gaps in the treatment of liquidity risk within Basel III Pillar II requirements.

The last article is by Jeroen Hofman (Front Office Quant, ING bank), who motivates the development of a Graphical Processing Unit (GPU) application for estimation of liabilities in a particular class of variable annuity products, namely the Single Premium Variable Annuities (SPVAs).

We hope you will enjoy reading this newsletter and we look forward to seeing you at the upcoming TopQuants event(s).

Aneesh Venkatraman

(on behalf of TopQuants)

#### Editorial Complex Financial Products: The Leing on

Products:	The	Icing on
the Cake		

Lévy copulas: Basic ideas and a new estimation method

Replication of a Class 5 of Variable Annuities for the Purpose of Economic Capital Calculations

<u>Variable Annuities</u> <u>Observations on valua-</u> <u>tions and risk manage-</u> <u>ment</u>

Pension Fund — Asset **7** Risk Management

Stress Testing: A theoretical exercise or does it actually work ?

<u>Stochastic Grid Bun-</u> <u>dling Method: A Tuto-</u> <u>rial</u>

Achieving super-fast convergence in Least Squares Monte-Carlo

<u>Global Model Practice</u> **I3** <u>Survey 2014: Validation</u> <u>at Risk</u>

Robustness of Expected15Shortfall and Value-at-Risk in a FilteredHistorical Simulation

Liquidity Risk Management in Europe: Baseline Basel III Pillar II by Dutch ILAAP

<u>SPVAs: A Grid GPU</u> 24 <u>Implementation</u>

#### **TopQuants Newsletter**

#### **Complex Financial Products: The Icing on the Cake** - written by Jon Vogelzang and Jantine Koebrugge (DNB)

**DNB**) and Jantine Koebrugge (Policy Advisor, Financial Risk Management, DNB) are a part of for the European Single Superviprovide a brief overview of the work involved and share their personal experiences as being a part of this project.

**Jon Vogelzang (Supervisor, Risk** The national competent authorities and Asset Liability Management, (NCAs) of several countries participate in this project amongst which is also the De Nederlandsche Bank (DNB).

the team within DNB that is in- Jon Vogelzang is an econometrician and volved in the preparatory work currently works as financial risk manager for DNB. Prior to that, he worked sory Mechanism. Together, they for the PGGM pension fund company and with ABN AMRO bank. Jon is closely involved in the asset quality review that DNB performs at the seven 'significant' banks in the Nether-



check the valuation of more complex and illiquid products (e.g. level 3 bonds, securitisations etc) and the pricing models of derivatives. We do this based on the guidelines set by the European Central Bank (ECB). It is an impressive 300-page document with templates that prescribe, which products have to be considered and on which basis we have to assess them."

Over the past three months, the



The European Banking Union will become effective from November 4th 2014 onwards. To begin with a clean slate, the balance sheets of all large banks in the euro zone countries will be assessed as part of the so-called Comprehensive Assessment Project.

lands. This is the part of the comprehensive assessment project which is aimed at assessment of the balance sheet and capital position of banks.

Jon: "The role of my team in this Jon: "We agreed with the ECB on project is to assess the fair value portfolios of the banks. It is our task to folios. Next, we can focus on the

team of lon was mostly focussed on selection of those products and the pricing models that exhibit the most valuation risk.

the selection of products and port-

#### Page 2

assets and begin the investigation process. For us, the complex financial products are the icing on the cake. These are mostly illiquid products for which no market values are observed. Using different models, we try to estimate the market value of these products which is quite challenging. What makes it more interesting is that, every product is different and hence we will have to employ new models all the time in order to get as close as possible to its "true" value."

The ECB had decided that securitisations, mostly being repackaged mortgages, will have to be valued by a third party. A good valuation team requires people who are capable of understanding the complexities involved in those products.

**Jon:** "Our team consists of seven quants, all from different departments in DNB. We work closely together and discuss the possible approaches which makes this project a great fun. By the end of June, we hope to have finalised the Asset Quality Review (AQR), which will be used as input for the stress tests."

#### Stress testing

The stress test forms the final phase in the comprehensive assessment project. Jantine Koebrugge has been involved from the start in this project. She had joined DNB three years ago, her first job in the industry after having obtained her masters in financial mathematics from University of Groningen.

#### Disclaimer

**Jantine:** "The stress tests are developed in close cooperation with the European Banking Authority (EBA). This requires a lot of knowledge on banking regulations and the models that banks use for the stress tests."

The scenarios for stress testing are developed based on the economical expectations of the European Commission.

Jantine: "An example of a stress scenario would be, increasing unemployment rates. Banks would use this scenario to calculate the future impact on their positions, for instance, where will they possibly be in three years from now. These scenarios are the same for each bank in Europe, although the implementation of the stress test is done individually by the banks. Every bank develops its own models for this purpose and uses their own data."

**Jon:** "The Asset Quality Review ensures that all banks have valued their asset in a similar manner, resulting in the same starting point for each 'significant' bank in Europe. In this way, we avoid comparing apples with oranges."

**Jantine:** "The ECB quality assurance team benchmarks the results across countries to ensure quality and consistency of the analysis as much as possible."

**Jantine:** "What I like about this project is that, the targets are clearly set

and we know the 'head' and 'tail' of it. Further, we encounter many challenges that we address together as a team. Working with different people is another reason why I enjoy being a part of this project."

Any articles contained in this newsletter express the views and opinions of their authors as indicated, and not necessarily that of TopQuants. Likewise, in the summary of talks presented at TopQuants workshop, we strive to provide a faithful reflection of the speaker's opinion, but again the views expressed are those of the author of the particular article but not necessarily that of TopQuants. While every effort has been made to ensure correctness of the information provided within the newsletter, errors may occur in which case, it is purely unintentional and we apologize in advance. The newsletter is solely intended towards sharing of knowledge with the quantitative community in the Netherlands and TopQuants excludes all liability which relates to direct or indirect usage of the contents in this newsletter.

#### **TopQuants Newsletter**

#### Lévy copulas: Basic ideas and a new estimation method

- based on talk by Joris van Velsen (ABN AMRO)



"A new method to select and estimate a Lévy copula for a discretely observed compound Poisson process is presented. The methodology enables the Lévy copula to become a realistic tool of the advanced measurement approach for operational risk." — Joris van Velsen

an important role in financial modelling, although the concept of a Lévy copula is comparatively less well known. In essence, a Lévy copula provides the relationship between the Lévy measure of a multivariate Lévy process and the Lévy measures of the associated marginal processes. The key application of a Lévy copula is to parsimoniously specify a multivariate Lévy jump process via a bottom-up approach.Against this background, the speaker focussed on presenting the theory of Lévy copulas and their financial applications.

Distributional copulas play

The presentation consisted of two parts. Firstly, the speaker, Joris van Velsen, gave a general introduction of Lévy copulas and discussed some important applicationsfrom literature, such as multi-asset option pricing.Secondly, the speaker presented a new method to select and estimate a Lévy copula for a discretely observed compound Poisson process. The speaker emphasized the usefulness of this method in the area of operational risk modelling.

To motivate his research, the speaker began by discussing the industry practice of operational risk modelling, which is typically done by adopting a threestep approach. Firstly, banks on business line and event method has successfully been type. Next, the loss in each applied to actual loss data. category is modelled by a Technical details about the compound Poisson process. method can be found in the Finally, the annual losses of pre-print different categories are connected by a distributional copula. The speaker then The presentation was well explained the advantages of a received and resulted in lively Lévy copula over a distribu- discussions about possible tional copula in the context extensions of the method and of operational risk modelling. Firstly, with a Lévy copula, tion on the same subject had the nature of the model is previously been given by the invariant with respect to the speaker at the 2012 Analytics level of granularity (i.e.\_if two Forum of the Operational loss categories are merged, Risk data exchange (ORX) the loss process of the new association, a world-wide category is again a com- consortium of banks dedipound Poisson process). cated to advancing the meas-Secondly, a Lévy copula allows for a natural interpretation of dependence between loss categories in terms of conclude a part-time study common shocks.

Lévy loss categories has been the programme, the speaker studied in the literature in received the Best Students case of known common Award for Risk Management. shocks (this corresponds to continuous observation). In practice, however, this information is typically not available in operational loss databases. The speaker highlighted his research work which had resulted in developing a method to estimate and select a Lévy copula of a discretely observed bivariate compound Poisson process. Simulation results indicated that the method works well for sample sizes typically encountered in operational

identify loss categories based risk modelling. Further, the http://arxiv.org/ pdf/1212.0092.pdf.

future research. A presentaurement and management of operational risk. The speaker performed the research to Risk Management at the Duisenberg school of finance Estimation and selection of a (DSF) from 2010 to 2012. copula between two For his performance during

> — summarized by Joris van Velsen

#### **Replication of a Class of Variable Annuities for** the Purpose of Economic Capital Calculations - based on talk by Roald Waaijer and Dimphy Hermans (Deloitte)

In recent years, life insurance companies increasingly started using replicating portfolio techniques for calculating economic capital. Key difficulties occur in the replication of complex insurance products with pathdependent guarantees, such as variable annuity products. The speakers, Roald Waaijer and Dimphy Hermans from Deloitte FRM, the department of Deloitte that focuses on financial risk management solutions for financial institutions, discussed the replication of complex insurance products by means of vanilla instruments using a data mining technique and compared it with replication using exotic options. This presentation included a general discussion on the use of replicating portfolios for economic capital calculations and the difficulties in replicating variable annuity products, the visualisation of a data mining technique and a case study comparing the results of two different replication approaches.

Deloitte has observed that insurance companies employing replicating portfolio techniques do manage to replicate the path-independent cash flow portion of their portfolio. However, several difficulties are experienced when replicating products with path-dependent cash flows, for instance in the case with variable annuities. Solvency II and EIOPA have emprovide a series of payments to the policyholder during derlying investment account.

using two different ap- vanilla instruments. proaches. In the first approach, only between the annuity and the still resulted in an imperfect variable annuities. replication of the cash flows. The second approach allowed the insurer to use both vanilla instruments and path-dependent options for replication, which resulted in a more intuitive replicating portfolio.

The speakers then showed

phasized the difficulty in the outcomes of a case study replicating these products as in which the two different well. Variable annuities are approaches were compared. It insurance products that was shown that in case the variable annuity was further simplified, a perfect replication the entire fixed term of the could be found using the secpolicy or, until the death of ond approach while in case of the policyholder in case of a no further simplification, no life annuity. The level of perfect replication was found. these payments depends on However, the use of paththe performance of the un- dependent instruments still resulted in a better in-sample replication quality and a better For illustration purposes, sensitivity match between the the speakers presented rep- replicating portfolio and the lication of a specific variable variable annuity when comannuity product, performed pared with using only plain

**Deloitte**.

(path- The talk was very well reindependent) vanilla instru- ceived by the audience and led ments were used for the to a lively discussion, which replication. Using cash flow included the computational analysis, a likely candidate cost involved in using pathasset set consisting of plain dependent options for replicavanilla instruments was se- tion. The overall conclusion lected. Due to the mismatch was that, while a closed-form path - valuation formula is not availindependent instruments able for every path-dependent and the path-dependent instrument, the approach alproduct, a data mining ap- lowing path-dependent instruproach was required. How- ments in the replicating portever, the difference in risk folio results in a more intuitive profile between the variable instrument selection and replipath- cating portfolios that better independent instruments capture the sensitivities of

> — summarized by Roald Waaijer and Dimphy Hermans

"Allowing path dependent instruments in the replicating portfolio results in a more intuitive instrument selection and replicating portfolios that better capture the sensitivities of variable annuities" - Roald Waaijer and **Dimphy Hermans** 

#### **TopQuants Newsletter**



#### Variable Annuities — Observations on valuations and risk management - based on talk by David Schrager (ING)

"We can focus as much as we want on more and more sophisticated models, but if we cannot get the simple vanilla products right, we are already mispricing things to such a large extent that the typical profit margin on such products quickly evaporates" — David Schrager

increasingly become a widely used instrument in retirement planning, especially in countries like America and lapan where it amounts to billions of euros of premiums every year. Further, there is expected to be increasing products right, we are aldemand for VA in the future as more people, particularly from developed countries live longer healthier lives. In short, VA are the answer to the demand for private (3rd pillar) pension products. Against this background, the speaker David Schrager, Single Premium Variable Annuity Trading at ING Bank, had contributed with a presentation on variable annuities which included a general introduction to VA, note on industry practices for their valuation and hedging and how to efficiently deal with policyholder behaviour in the valuation of these products.

There were few other talks on VA during the TopQuants workshop. In particular, the talk by Roald Waaijer and Dimphy Hermans focussed more on how to replicate a VA using existing instruments in order to speed up economic capital calculations while David Schrager had focussed on two important aspects of the pricing of VAs; from the guarantee embedbasis risk arising due to wrong choice of discount Based on this functional curve and behavioural or lapse risk arising due to the client's early surrender.

Variable Annuities (VA) have The speaker emphasised on these two points in a very lively and interesting manner. According to him, we can focus as much as we want on more and more sophisticated models, but if we cannot get the simple vanilla ready mispricing things to such a large extent that the typical profit margin on such products quickly evaporates. An important point to be kept in mind is that the forward price of assets has to include the repo rate, as has been pointed out in many technical papers that were written since the crisis, for instance refer to e.g. Piterbarg. The widening crosscurrency basis is another factor to take into account. Secondly, behavioural or lapse risk is pivotal to the valuation of VAs and it should also be taken into account in such products. It is wrong to assume that clients will walk away from their variable annuity contracts in a rational manner. The speaker highlighted his research work done together with the co-authors in which they have attempted to model this lapse behaviour in a simple manner based on how much the current market levels differ ded within the contract. form, one can attempt to structure financial derivatives ("building blocks") from which the value of the vari-



able annuity can be built. If values of these building blocks can be obtained in the market, it will facilitate the pricing of VAs. The estimation of the degree of irrationality however remains, and is an important risk in these products.

The speaker concluded the talk by presenting an illustrative case study that involved hedging of VAs. Overall, the talk was well received by the audience and had led to a lively after discussion.

— summarized by

Roger Lord and

Aneesh Venkatraman

#### Pension Fund — Asset Risk Management - based on talk by Tony de Graaf (PGGM)

governance from their delegated investment managers. They prescribe detailed to receive comprehensive ment portfolios, certainly on the risk side. The speaker, Tony de Graaf, had discussed several popular investment risk reporting items and offered some new ideas, focusing mainly on the public markets investment During the 2008 crisis, some portfolios. A short summary toolbox, but certainly not an exhaustive set.

## ment

Investment managers sometimes have a tendency to narrow their focus on certain portfolios, especially ever, pension fund boards always look first to obtain a risk report that gives them immediate insight into the main risks of their fund. Risk attribution is a useful tool regard, the speaker has de-

Currently, there is an in- idea of how volatile their cov- tistics like Value-at-Risk, creasing need for pension erage ratio is: the Coverage fund boards to be 'in con- Ratio at Risk (CRaR). This trol', perhaps much more statistic presents the worst lar to the more commonly than it previously used to coverage ratio that the board be. They demand, among can expect within a given cermany things, transparency, tain horizon and confidence robust processes and good level. The CRaR can be attributed to different asset classes and/or different investment decisions. Typically an ALM compliance rules and expect study comes first followed by the Strategic Benchmark and reporting on their invest- finally the implementation. For each of these decisions and each step in the investment process, the effect on the CRaR can be determined.

#### Liquidity and controllability

pension funds were conof these risk reporting ele- fronted with liquidity conments is provided, which straints, especially when they should be considered as a had implemented large derivative overlay structures. The speaker presented a risk dashboard which shows for a Balance sheet risk measure- certain stress scenario, the required or available liquidity for each asset class and overlay, including the effects of possible repo market actions and rebalancing schemes. Controllability then measures when they manage only part to what extent the resulting of the pension assets. How- asset mix can be steered back to the strategic mix.

#### **Risk** attribution

Coverage ratio is a very for risk managers that can be important financial statistic applied in very different setemployed by pension funds tings. The speaker highlighted in the Netherlands. In this its use in balance sheet risk management and presented veloped a dashboard that the mechanics of risk attribugives pension board a good tion for widely used risk sta-



Tracking Error, Expected Shortfall, in a way that is simiused technique of performance attribution. Risk and performance attribution measures complement each other and together they quantify all investment decisions made by a portfolio manager, from both a risk and a return perspective. The total risk and performance can be attributed to allocation and selections decisions, to risk types, country/region, style, strategy, instrument type etc. These attributions can be calculated either separately or can also be nested, e.g. first performing allocation/ selection and then attribution to the different regions where the portfolio manager invests. The speaker presented this for both the classical approach and a new approach formulated by himself. This new method provides more flexibility and intuitive outcomes, although being more computationally intensive.

Other topics discussed include stress testing, style analysis, AIFMD. The speaker engaged with the audience on topics like technologies used in these Risk Management toolkits, calculation run time, applicability of the tools for non-linear products, systematic risk coverage within the risk management tool etc.

> summarized by Tony de Graaf

**"Financial risk** measurements within asset management only become fully useful when combined with methods able to zoom in, top down, and show the risk contributions made by the various components and decisions made in the investment management process"

— Tony de Graaf

#### Stress Testing: A theoretical exercise or does it actually work? — by Robert Daniels (Partner at Capstone Financial Industry)



Why are we surprised when the outcome of a stress scenario is far worse than what was predicted? Often we tend to rationalize the outcome e.g. "it was a four sigma event" or "it was a black swan". However, could it be the case that the applied stress test methodologies are inherently weak? If so, how can a risk modeler/manager communicate these weaknesses to senior management or even on a board level? In this article an overview is given of commonly applied stress test methodologies including some practical challenges for risk modelers and risk managers.

## Stress tests are widely performed for many years so what is new?

This is true. Many organizations are performing stress tests as part of their standard risk management framework. However during the recent crises the limitations of these stress tests have been revealed e.g. for several portfolios a Value-at-Risk of losses under stress tests were estimated of less than a million, whilst actual losses exceeded several billions. Therefore, one of the questions that is on the table is how a framework can be setup that aims at identifying weaknesses under stressed circumstances.

## Combining macro-economic and risk models for stress testing: The Holy Grail or a recipe for disaster?

One of the most commonly applied stress test methodologies is to relate macro-economic variables to risk parameters and based on these risk parameters the stress impact is assessed. Even though this approach seems logical it is an inherent weak approach. Both macro-economic and risk models are weak to predict the impact of stressed circumstances and lead to a situation as illustrated in this figure below.



But what is driving this disconnect? Macro-economic models are known for their weak predictiveness, even under normal circumstances. In addition, there are factors that play an important role during times of stress for example hidden (contractual) optionalities, non-linearities in pay-off structures and behavior of financial markets and market participants. Surprisingly, these factors are often forgotten by (quantitative) risk managers even though they drive the outcome under stress significantly.

#### The "Risk management please provide one number for the outcome of a stress test" syndrome

If you often perform stress tests then you know what I am talking about. Senior management often requires risk management to provide a clear, one figure impact of a stress test. From my experience this approach gives a false sense of security to senior management. Also a one figure impact does not provide senior management the right tools to timely mitigate the effects if an event occurs.

A different method would be to define multi-stage stress tests in which an event occurs in various stages. The benefit of this approach is that the impact for each stage can be estimated in terms of the balance sheet, P&L, markets and the business model itself. Besides focusing on the impact, it leads also to discussion on what to do when an event materializes. For example, can triggers be defined in an early stage such that a discussion takes place on the measures to be taken at that time?

This approach does require a lot of knowledge of course. Not only regarding risk models, but also from financial markets and behavior of market participants. The key of success is therefore in the creativity and knowledge of a risk manager when defining stress tests. On the other hand, blaming external factors such as "four-sigma events" or "black swans" are still tempting as little knowledge and no action is required.

Robert Daniels holds M.Sc. in financial econometrics and M. Phil in economics. He is partner at Capstone Financial Industry and Daniels Risk Advisory. His aim is to provide fundamentally sound solutions to financial institutions in the field of strategic risk management and effective decision making.



#### Stochastic Grid Bundling Method: A Tutorial

— by Cornelis Oosterlee (Delft University of Applied Mathematics)

#### Abstract

This note describes a practical simulation-based algorithm, which we call the Stochastic Grid Bundling Method (SGBM) for pricing multi-dimensional Bermudan (i.e. discretely exercisable) options. The method generates a direct estimator of the option price, an optimal earlyexercise policy as well as a lower bound value for the option price. An advantage of SGBM is that the method can be used directly to obtain the Greeks (i.e., derivatives with respect to the underlying spot prices, such as delta, gamma, etc) for Bermudan-style options. Computational results for various multi-dimensional Bermudan options, presented in [1], demonstrate the simplicity and efficiency of the algorithm proposed.

#### **Stochastic Grid Bundling Method**

A Bermudan option gives the holder the right, but not obligation, to exercise the option once, on a discretely spaced set of exercise dates. Pricing of Bermudan options, especially for multi-dimensional processes is a challenging problem owing to its path-dependent settings.

Consider an economy in discrete time defined up to a finite time horizon T. The market is defined by the filtered probability space

 $(\Omega, F, F_{\star}, Q).$ 

Let.

$$X_{t}$$
,  $t = t_{0}, \dots, t_{m} = T;$ 

be an  $R_d$  -valued discrete time Markov process that

describes the state of the economy, the price of the underlying assets and any other variables that affect the dynamics of the underlying. Here, Q is the risk neutral probability measure. The holder of the Bermudan option can exercise the option at any of the discrete times

$$t = t_0, \dots, t_m = T \tag{1.1}$$

CENT Centrum Wiskunde & Informatica

Let  $h(X_{\star})$  represent the cash flow received when the

option is exercised at t, with underlying state being  $X_t$ .

We define a policy,  $\pi$ , as a set of stopping times  $\tau$  which can assume any of the discrete time values in equation (1.1). The option value is found by solving an optimization problem, i.e. to find the optimal exercise policy,  $\pi$ , for which the expected cash flow is maximized. This can be written as:

$$V_{t_0}(X_{t_0}) = \sup_{\pi} E[h(X_{\tau})|X_{t_0}]$$
(1.2)

In simple terms, equation (1.2) states that of all possible exercise policies in the given decision horizon, the option value is the one which maximizes the expected future cash flows. SGBM solves a general optimal decision time problem using a hybrid of dynamic programming and Monte Carlo simulation. The steps involved in the SGBM algorithm, can be summarized as follows:

#### Step I: Generating grid points

The grid points in SGBM are generated by simulating independent copies of sample paths,

$$\{S_{t_0}(n), \dots, S_{t_M}(n)\}, \quad n = 1, \dots, N,$$

of the underlying process  $S_t$  and all starting from the

same initial state  ${S}_{t_0}$  The  $n^{th}$  grid point at time  $t_m$ 

is given by:

$$S_{t_m}(n)$$
  $n = 1, \dots, N.$ 

Depending upon the underlying process an appropriate discretization scheme, e.g. the Euler scheme, is used to generate sample paths. Sometimes the diffusion process can be simulated directly, essentially because it appears in a closed form, as an example, for the regular multidimensional Black-Scholes model.

#### Step II: Option value at terminal time

The option value at terminal time is given by:

$$V_{t_{m}}(S_{t_{m}}) = \max(h(S_{t_{m}}), 0)$$

This relation is used to compute the option value for all grid points at the final time step. The following steps are

subsequently performed for each time step,  $t_m$ ; with

 $m \leq M$ , recursively, moving backwards in time, starting

from t<sub>M.</sub>

#### Step III: Bundling

The grid points at  $t_{m-1}$  are bundled into

$$B_{t_{m-1}}(l), \dots, B_{t_{m-1}}(v)$$

non-overlapping sets or partitions. Three different approaches for partitioning are considered, they are:

- I. K means clustering algorithm,
- 2. Recursive bifurcation,
- 3. Recursive bifurcation of reduced state space.

These techniques are detailed in [1].

## Step IV: Mapping high-dimensional state space to a low-dimensional space

Corresponding to each bundle

$$B_{t_{m-1}}(\beta), \beta = l_{1, \dots, \nu}$$

a parameterized value function,  $Z: \mathbb{R}^d \times \mathbb{R}^K \to \mathbb{R}$ which assigns values  $Z(S_{t_m}, \alpha_{t_m}^{\beta})$  to states  $S_{t_m}$  is computed. Here,  $\alpha_{t_m}^{\beta} \in \mathbb{R}^K$  is a vector of free parameters. The objective is then to choose, for each  $t_m$ 

and  $\beta$ , a parameter vector  $\alpha_{t_m}^{\beta}$  so that

$$Z(S_{t_m}, \alpha_{t_m}^{\beta}) \approx V_{t_m}(S_{t_m}).$$

The parameter vector is determined by means of regression.

#### Step V: Computing the continuation and option

values at 
$$t_{m-1}$$

The continuation values for

$$S_{t_{m-1}}(n) \in B_{t_{m-1}}(\beta), n = 1, \dots, N, \beta = 1, \dots, \nu$$

are approximated by

$$\hat{Q}_{t_{m-1}}\left(S_{t_{m-1}}(n)\right) = \mathbb{E}[Z\left(S_{t_m}, \alpha_{t_m}^{\beta}\right) | S_{t_{m-1}}(n)]$$

The option value is then given by:

$$\hat{V}_{t_{m-1}}\left(S_{t_{m-1}}(n)\right) = \max[h\left(S_{t_{m-1}}(n)\right), \hat{Q}_{t_{m-1}}\left(S_{t_{m-1}}(n)\right)]$$

This procedure is repeated over all time steps, backward in time, until the initial time point  $t_0$  is reached.

#### References

[1] Shashi Jain and Cornelis Oosterlee, The Stochastic Grid Bundling Method: Efficient Pricing of Bermudan Options and their Greeks(September 4, 2013). Available at SSRN: http://ssrn.com/abstract=2293942

#### Achieving super-fast convergence in Least Squares Monte-Carlo

— by Eric Beutner, Antoon Pelsser, Janina Schweizer (Maastricht University)



#### Introduction

The Least Squares Monte Carlo (LSMC) technique is widely applied in the area of Finance, especially in pricing high-dimensional Bermudan/American-style options, where closed-form solutions are not available. Under LSMC the cross-sectional information inherent in the simulated data is exploited to obtain approximating functions to conditional expectations through performing least squares regressions on the simulated data. Simulation-based regression methods are also applied in insurance risk management as a technique to estimate the value of (Life and Health) insurance liabilities. Essentially these techniques are used to estimate unknown conditional expectations across time, which in Finance and insurance boils down to estimating the price of a contingent claim, for which closedform solutions are not available. In this article we discuss a particular LSMC estimator, for which convergence in mean square faster than  $N^{-1}$  can be achieved. This article is based on the key results in Beutner et al. (2013).

#### The point in time of regression matters!

The majority of the academic literature deals with LSMC estimators where the conditional expectation function (pricing function) at time t is estimated through least squares regression of the value function at a time point T against basis functions at an earlier time point t, t < T. The approach is known as Regression-Now (Glasserman and Yu, 2004). An alternative approach, termed Regression -Later, approximates the value function at time T through regression on basis functions measurable with respect to the information available at time T. The estimate for the price at time t is then obtained by pricing the basis functions. Although similar, Regress-Now and Regress-Later are fundamentally different.

- Regress-Later can achieve a convergence in mean-square that is faster than  $N^{-1}$  which Regress-Now cannot.
- The functions to be approximated with regression on the Monte Carlo simulation set may differ in nature.

In this article we address the first point.

#### The technical set-up

We consider here a very simple set-up and omit technical details. This should allow the reader to quickly see the difference between LSMC with Regress-Now and with Regress-Later. We restrict attention to contingent claims with finite second moments. This allows us to model the contingent claims in a Hilbert space. From Hilbert space theory we know that an element of a separable Hilbert space is expressible in terms of an infinite. but countable orthonormal basis. As we cannot estimate infinitely many parameters based on finite samples for estimation purposes the expression must be truncated. Thus, we can express X through a finite linear combination of basis functions plus an approximation error, which arises from truncating the basis. Now, recall that in Regress-Now the basis functions refer to an earlier time point t, t < T. By regressing X against basis functions at time t the conditional expectation with respect to information at time t is directly estimated. Then, additional to an approximation error a projection error is realized arising from the time-difference. Let X be the payoff at time T of a contingent claim. In a very simple set-up let Z(T) be the underlying random variable driving the random payoff X at time T. The basis functions are denoted by  $\mathcal{C}_i$ .

#### **Regression equation with Regress-Later**

$$X = \sum_{i=1}^{K} \alpha_i e_i (Z(T)) + err_1$$

**Regression equation with Regress-Now** 

$$X = \sum_{i=1}^{K} \alpha_i e_i (Z(t)) + err_1 + err_2$$

where  $PT_1$  and  $PT_2$  refer to approximation and projection error respectively. In estimating the above, the truncation parameter K is not fixed and finite but grows with the sample size. Thus, in the limit, the approximation error vanishes for both Regress-Now and Regress-Later.

#### **TopQuants Newsletter**

#### Super-fast convergence

The convergence rates in mean-square for Regress-Now and Regress-Later are functions of the sample size, N, and the number of basis terms, K(N). The explicit convergence rates below are taken from Beutner et al. (2013).

**Convergence rate for Regress-Later:** 

$$O_p(K(N)^{-\gamma_{lat}})$$

**Convergence rate for Regress-Now:** 

$$O\left(\frac{K(N)}{N}\right) + O_p(K(N)^{-\gamma_{now}})$$

The potential super-fast convergence in Regress-Later is achieved as the regression problem is non-standard. From the previous explanations we can see that the approximation error decreases as the sample size grows. This follows as the truncation parameter K is an increasing function of the sample size. In Regress-Now also the approximation error converges to zero as the sample size grows, but the projection error remains. We can see that the Regress-Now convergence rate has an additional term, which arises from the projection error. If the target function is in the span of finitely many basis functions the approximation error in Regress-Now vanishes and only the projection error is left. Then, the Regress-Now estimator converges at rate  $N^{-1}$ , which is its maximum convergence rate. The ultimate convergence rate of the Regress-Later estimator is given by the convergence rate stated above and the growth relation of the truncation parameter and the sample size. Note that intuitively the growth rate of K in relation to the sample size must be restricted as for a given sample size only a limited number of parameters can be estimated.

We illustrate the super-fast convergence with normalized non-overlapping piecewise linear functions, which are by construction orthonormal. In the first example we consider a hyperbolic function. In the second example we consider a stock modelled as a geometric Brownian motion. The underlying drivers are Brownian motions. In the first example a convergence rate of  $N^{-2}$  is achieved (see top figure), in the second case the convergence rate is still faster than  $N^{-1}$  (see bottom figure).



#### Conclusion

In this short article we discussed two types of LSMC, Regress-Now and Regress-Later, and illustrated that for Regress-Later convergence faster than  $N^{-1}$  can be achieved. This renders Regress-Later a very interesting alternative to the typically applied Regress-Now estimators in LSMC.

#### References

Beutner, E., Pelsser, A., and Schweizer, J. (2013). Fast convergence of Regress-Later estimates in Least Squares Monte Carlo. <u>http://papers.ssrn.com/sol3/papers.cfm?</u> <u>abstract\_id=2328709</u>. Working Paper.

Glasserman, P. and Yu, B. (2004). Simulation for American options: Regression now or regression later? In *Monte Carlo and Quasi-Monte Carlo Methods 2002*, pages 213-226. Springer Berlin Heidelberg.

Deloitte.

#### Global Model Practice Survey 2014: Validation at Risk

— by Florian Reuter and Arjan de Ridder (Deloitte Financial Risk Management)

#### Introduction

Increasing model complexity has given rise to a new type of risk faced by financial institutions: model risk. Both regulatory regimes and financial institutions have taken steps to address this type of risk. The cornerstone in managing model risk is an independent Model Validation function. Model Validation provides an objective review to Model Development, hence addressing the issue of model risk. Furthermore, Model Validation plays an important role in assessing the compliance of models to internal and external regulations. As a result, Model Validation provides comfort to the stakeholders in the use of the models and thereby improves model-based decision making within an organization. Currently, the practices of Model Validation activities vary among financial institutions.

Every two years, Deloitte conducts the Global Model Practice Survey (GMPS) a global survey on model practices within financial institutions. The latest edition of the survey was conducted in the second half of 2013 and focused on the state of the Model Validation function within financial institutions. The survey was conducted among 96 financial institutions globally, of which 15 based in The Netherlands. The respondents represent different geographies, industries, sizes and structures. Based on the completed set of responses we provide insight into the operation of Model Validation within various organizations. The key findings of the survey are listed below.

#### Model Validation has become an established practice

The added value of Model Validation for the business is being increasingly recognized, i.e. all survey respondents indicated that Model Validation adds value and the majority of the respondents acknowledge the technical expertise of Model Validation. Other functions, such as Risk Management and Model Development, also recognize the important role of Model Validation as mitigant of model risk. On the other hand, the most frequently cited reason for having a Model Validation function is still regulatory compliance. Figure 1 presents the added value of Model Validation for the business, as perceived by Model Validation and other roles. Here, we see a misalignment in perception of Model Validation versus its stakeholders regarding the value added by Model Validation.



#### Figure I: Perceived added value of Model Validation for the business

The survey results demonstrate that Model Validation processes are becoming more mature and standardized. Compared to the GMPS 2011, significantly more respondents indicate that the ownership of the model inventory is formalized. This development improves the oversight of the model landscape within the financial institutions and herewith also the control framework.

#### However, it is still not a mature activity

Despite the achievements made over the last two years, there is still significant room for improvement. Many respondents indicate that Model Validation is still at its infant stage. Difficulties are experienced in adhering to the model validation cycle and the advice of Model Validation to reject or substantially remediate a model, is often not followed. In addition, defining and documenting roles and responsibilities of Model Validation is considered to be challenging. In particular, for institutions with a decentralized Model Validation function or financial institutions without an independent Model Validation function, these roles and responsibilities are often not adequately documented.

The survey results indicate that in many cases Model Validation only covers regulatory models and that these models require more personnel to cover the desired scope. In addition, in order to be compliant with (future) regulations, a substantial part of the respondents would like to broaden the scope of activities performed by Model Validation. For example, by expanding the use of validation tools. Figure I shows an overview of validation tools currently used by the respondents.



Figure 2: Average percentages of validation tools used by the aggregate financial industry

Respondents also indicate that they would like to increase the size of the team. Although respondents repeatedly state that Model Validation is "an under-staffed function", it is also frequently considered to be an "expensive function constrained by available resources". Partially due to these (temporary) insufficient resources, about half of the respondents outsource model validation work to external parties.

Finally, the current state of performance assessment of the Model Validation function does not indicate a sufficient maturity of the function. In particular, a quarter of the respondents indicate to have no Key Performance Indicators for Model Validation.

#### Model Validation within banks is more mature than within other industries

Model Validation appears to be more mature at banks than at other institutions. Almost all banks have a centralized Model Validation function within the domain of Risk Management. Other industries often have a decentralized Model Validation function where responsibilities are less clearly defined or do not have an independent Model Validation function at all. Banks also assign on average more FTE resources to Model Validation although the average model validation working experience is lower for banks. Larger departments (more common for banks) seem to have relatively fewer seniors and more juniors.

#### Going forward

We asked the respondents to provide their vision on the development of the Model Validation function in the next three years. The general consensus is similar to the survey of 2011: the respondents believe the importance and prominence of Model Validation to continue to increase in the future. Varying reasons for the increasing importance

and prominence are provided. One is the continued increase in regulatory expectations for Model Validation. The regulation of financial institutions is expected to become even more stringent. Banks today still face challenges in implementing Basel II whereas Basel III is already imminent. The European insurers have to comply with Solvency II directive while upcoming and existing regulation for investment managers, pension funds and other financial institutions is increasing both in aggregate and with greater emphasis on quantitative requirements.

"The value and importance of model validation will further rise because of new regulatory requirements"

Group Manager of Risk Model Validation department of a bank

**Deloitte** 

Finally, the survey results indicate that the main challenge faced by Model Validation is to move from a predominantly compliance function into a business partner which proactively manages model risk and ultimately promotes better usage of models within an organization. The full report can be found <u>here.</u>

#### Robustness of Expected Shortfall and Value-at-Risk in a Filtered Historical Simulation Framework

— by Gerdie Knijp and Niek Crezée (Deloitte Financial Risk Management)

#### Introduction

One of the objectives of the Basel Committee is ensuring consistency of market risk-weighted asset (mRWA) outcomes. Recently several regulators (BIS and IMF) have published papers (Basel Committee on Banking Supervision, 2013), (Avramova & Le Leslé, 2012), in which they show that the mRWAs calculated for similar portfolios differ across countries and banks. These variations are not only due to different risk profiles or different supervisory rules but it is presumed that a significant part of the variability in mRWAs is caused by different methodology choices of banks. This negatively affects market confidence and therefore there is need for a revision in the regulatory framework.

At the same time, the Basel Committee on Banking Supervision (BCBS) presents a number of propositions for a revision of the trading book (Basel Committee on Banking Supervision, 2013), as it is recognised that the old framework has some significant shortcomings. One of the considerations described in the second consultative document of the Fundamental Review of the Trading Book, is a change of the market risk metric on which the mRWAs should be determined in an internal model based approach. BCBS proposes the use of expected shortfall (ES) at a 97.5% confidence interval as an alternative for the widely used value-at-risk (VaR), measured at a 99% confidence interval.

Whereas VaR simply measures the quantile of the loss distribution, ES measures the expected loss of a portfolio given that the loss has exceeded a certain quantile. It therefore takes tail risk into account. Following the Basel propositions, we compare a 99% VaR with a 97.5% ES. This comparison stems from the normal distribution, as the two are approximately equal if the underlying distribution is normal.

Considering the observed variability in mRWAs measured under VaR, we analyse the sensitivities of certain assumptions on the VaR and ES measures. Particularly now that ES is proposed as replacement for VaR, we consider it worthwhile to investigate how this transition would affect the consistency of mRWAs among firms with similar risk profiles. We will analyse the robustness of VaR and ES, where we define robustness as the sensitivity of market risk measures towards certain model choices or assumption changes in a model.

#### **Filtered Historical Simulation**

We use filtered historical simulation (FHS) to calculate VaR and ES. FHS is a widely acknowledged method in (academic) literature. It is a semi-parametric technique which uses bootstrapping and combines historical simulation with conditional volatility modelling. FHS takes volatility clustering into account which makes it a more advanced

#### Page 15

method than simple historical simulation. FHS generates scenarios of risk factor returns from which VaR and ES can be calculated.

We include several conditional volatility models, namely a simple GARCH model, the asymmetric GJR-GARCH model and an EWMA model, which is used in RiskMetrics, as these models have proven to work well in practice and are commonly used within financial institutions. These models cover symmetric and asymmetric conditional volatility models and models with and without mean reversion.

#### **Empirical analysis**

We constructed a portfolio consisting of simple equity and fixed income products. Risk factors to which these products are exposed are equity indices, short- and long-term interest rates and short- and long-term credit spreads for different credit ratings.

The main analysis of robustness of VaR and ES is done by investigating the sensitivity of these risk measures towards parameter modifications. We perform small modifications towards the different parameters underlying the conditional volatility models and investigate the effect on VaR and ES using the theory of influence functions (Hampel, et al., 2011). Influence functions are widely used in robustness analysis and can easily be adapted towards our investigation purpose. This influence curve is defined by:

$$IC(\hat{\theta}_{k}, F_{L}, T) = \lim_{\epsilon \to 0} \frac{T\left(\hat{F}_{L}(\hat{\theta}_{k} + \epsilon)\right) - T\left(\hat{F}_{L}(\hat{\theta}_{k} - \epsilon)\right)}{2\epsilon},$$

where  $\hat{\theta}_k$  represents a certain estimated parameter in the conditional volatility model,  $\hat{F}_L$  is the empirical loss

function followed from the FHS process and T is a statistic which is in our case VaR or ES.

We calculate approximations of the influence functions with respect to different parameter changes for VaR and ES at different points in time. This gives us a time series of sensitivity estimates for both VaR and ES for different parameters. We make a distinction in sensitivity effects due to changes in parameters in short-term interest models, long-term interest models and equity.

Figure I shows such a time series of the influence curve, based on a change in  $\lambda$  in the EWMA model for long term interest. From the pattern observed, we see that the sensitivity of VaR can become much more extreme than sensitivity of ES. For other parameters, asset classes and models, similar patterns occur, from which we expect VaR being more sensitive towards small parameter modifications than ES.

To confirm this hypothesis, we perform simple linear regressions on the difference of the absolute value of the sensitivity parameter of VaR and ES over time. We analysed the effect of changes in different estimated parameters from

the conditional volatility models, namely  $\hat{\theta} = (\hat{\alpha}_1, \hat{\beta}_1, \hat{\gamma}, \lambda)$  The estimated parameters for the different conditional volatility models are: (I) GARCH (I,I)  $h_t = \alpha_0 + \alpha_1 a_{t-1}^2 + \beta_1 h_{t-1}$  (2) EWMA(I,I):  $h_t = (1 - \lambda)r_{t-1}^2 + \lambda h_{t-1}$  (3) GJR - GARCH(I,):  $h_t = \alpha_0 + (\alpha_1 + \gamma \ 1_{\{a_{t-1} < 0\}})a_{t-1}^2 + \beta_1 h_{t-1}$ 

We formulated two hypotheses to test for differences in robustness properties of VaR and ES. We first test whether the difference of the absolute values of the influence function of VaR and ES is equal to zero or not:

$$\begin{split} H_0^1 &: E[|IC_t(\hat{\theta}_k, VaR)| - |IC_t(\hat{\theta}_k, ES)|] = 0, \\ H_1^1 &: E[|IC_t(\hat{\theta}_k, VaR)| - |IC_t(\hat{\theta}_k, ES)|] = \mu \neq 0. \end{split}$$



Figure 1: Time series of the influence curve of VaR en ES based on modifications in  $\lambda$  in the EWMA model for long term interest

This is done by regressing the difference of the absolute values of the influence functions of VaR and ES on a constant. By performing a t-test on the estimated intercept we test whether the estimated difference in absolute values of the influence functions of both measures is zero or not. We take into account that the residuals are possibly subject to autocorrelation and heteroskedasticity and therefore we use Newey-West standard errors. We find that this hypothesis can be rejected for all parameters, asset classes and models, meaning that there is enough evidence to state that the difference between the absolute value of the influence functions of VaR and ES is significantly different from zero. From the estimated coefficients, the patterns of the influence functions and the corresponding summary statistics, we can conclude that VaR is more sensitive towards parameter modifications than ES in a FHS framework.

Second, we test for dependence of this difference on conditional volatility, by defining a second hypothesis:

# $$\begin{split} H_0^2 &: E\left[\left|IC_t(\hat{\theta}_k, VaR)\right| - \left|IC_t(\hat{\theta}_k, ES)\right|\right| h_t\right] = 0, \\ H_1^2 &: E\left[\left|IC_t(\hat{\theta}_k, VaR)\right| - \left|IC_t(\hat{\theta}_k, ES)\right|\right| h_t\right] = c + \beta h_t, \end{split}$$

with either the intercept  $c \neq 0$ , the coefficient  $\beta \neq 0$ , or both. The parameter  $h_t$  represents the conditional volatility

at time *t*. This hypothesis is tested by performing a linear regression where we also regress on the corresponding conditional volatility. By performing both t-tests and an F-test on the estimated coefficients we test whether there is evidence for the difference of the absolute values of VaR and ES being dependent on conditional volatility. From the

regression results regarding  $H_0^2$  we again find that VaR is more sensitive towards small parameter modifications than

ES. Moreover, there is some evidence for the difference in absolute value of the influence functions of the two

measures being dependent on conditional volatility. However, this effect is not unambiguous for the different parameters, models and asset classes.

#### **Concluding remarks**

The result that VaR is less robust than ES is not in line with earlier studies. In literature it is proven that historical ES is unbounded in terms of the addition of extreme observations and thus more sensitive to extreme outliers than VaR (Cont, et al., 2010). However, VaR and ES are often compared at the same confidence level. Also, robustness is often investigated by means of sensitivity analysis where extreme observations are added to a dataset, rather than by means of modifications in model assumptions. We executed a different, more realistic, approach to test for robustness, since we constructed a portfolio for which VaR and ES are calculated using historical data of risk factors.

Our analysis showed that ES is less sensitive towards certain model choices, indicating mRWAs are less likely to vary a lot among banks with similar profiles when ES is used as a market risk metric.

#### **Bibliography**

Avramova, V. & Le Leslé, S., 2012. Revisiting risk-weighted assets. International monetary fund (IMF).

Basel Committee on Banking Supervision, 2013. Fundamental review of the trading book: A revised market risk framework.

Basel Committee on Banking Supervision, 2013. Regulatory consistency assessment programme (RCAP): an analysis of risk weighted of market risk.

Cont, R., Deguest, R. & Scandolo, G., 2010. Robustness and sensitivity analysis of risk measurement procedures. *Quantitative Finance*, 10(6), pp. 593-606.

Hampel, F., Ronchetti, E., Rousseeuw, P. & Stahel, W., 2011. Robust statistics: the approach based on influence functions. John Wiley & Sons.

#### Liquidity Risk Management in Europe: Baseline Basel III Pillar II by Dutch ILAAP

— by Elmo Olieslagers, Bert-Jan Nauta, Aron Kalsbeek (Double Effect)



Elmo Olieslagers (General Manager, Double Effect Germany,), Bert-Jan Nauta (Current Head of Economic Capital Modelling at Royal Bank of Scotland and previously Director Risk of Double Effect), Aron Kalsbeek (Risk Consultant, Double Effect) together present a working paper on Risk/ALM. The authors would like to acknowledge Kirsten Alink, Martin Koudstaal and Jill Brouwer for their important contributions towards this working paper.

#### Baseline Basel III Pillar 2 by Dutch ILAAP

The Dutch Central Bank (hereafter "DNB") has introduced the Internal Liquidity Adequacy Assessment Process (hereafter "ILAAP") in the Netherlands in June 2011. ILAAP has been introduced in addition to Basel III / CRD IV and its Liquidity Coverage Ratio (hereafter "LCR"), Net Stable Funding Ratio (hereafter "NSFR") and other liquidity risk management monitoring tools.

DNB requires banks to setup a recurring Internal Liquidity Adequacy Assessment Process whereby the bank thoroughly evaluates its liquidity risk management function. The qualitative and quantitative criteria's of Dutch ILAAP are based upon guidelines and principles. The guidelines and principles are put forward in various papers and other related pieces of advice, directives from the Basel Committee on Banking Supervision (hereafter "BCBS") and the European Banking Authority (hereafter "EBA").

We note that the treatment of liquidity risk in Pillar 2 (also called the "Supervisory Review Process") is lacking in Europe. In Pillar 2 there are no specific requirements for management of liquidity risk as there are for other type of risks (Note that liquidity risk is a far more important risk for a bank than solvency risk (Van der Wielen and Nauta, 2013). Theoretically, Diamond and Rajan (2005) have also emphasized the important interactions between liquidity and solvency, and how they can cause each other). Since, in Internal Capital Adequacy Assessment Process (hereafter "ICAAP") there are no specific requirements for management of liquidity risk as there is for other type of risks. And the Basel III guidelines for liquidity risk management in "Supervisory Review Evaluation Process" (hereafter "SREP") do not go into a very detailed level.

We recommend that the Dutch ILAAP self-assessment and rulebook procedure should function as a base line to mitigate a critical gap present in Pillar 2 of the Basel III framework.

#### Why use Dutch ILAAP as baseline?

- **Single comprehensive overview** of necessary elements to have a robust liquidity risk management function in place, based upon best practices from BCBS and EBA. This reduces search cost and ambiguity on what to regard "best practice".
- Mature set of operational liquidity rules that have been continuously improved since 2011 resulting from valuable interactions between DNB, banks and consultancy firms active in The Netherlands. The discussions are regarding translating operational implications of BCBS and EBA liquidity principles to concrete functional, technical and data requirements.
- **Proven methodology:** Financial institutions already report ILAAP to DNB in a similar way as in the context of the ICAAP/SREP since 2011.

#### What the Dutch ILAAP is about

In June 2011, the Dutch Central Bank (DNB) introduced the Dutch ILAAP via the Liquidity Policy Rule (Financial Supervision Act) 2011 (Beleidsregel liquiditeit Wft 2011). ILAAP is designed to ensure a robust management of liquidity risk within Dutch financial institutions.

ILAAP is the Dutch implementation of the September 2008 publication 'Principles for Sound Liquidity Risk Management and Supervision' and other related pieces of advice, directives of the BCBS and the EBA (formerly known as CEBS). ILAAP clarifies what can be considered "best practices" (for Dutch banks) with regard to the management of liquidity risk.

Two crucial elements of ILAAP are:

- The rulebook, which describes how the DNB will carry out its evaluation of ILAAP
- The self-assessment procedure which banks must carry out to assess their liquidity risk management and e.g. the related procedures, governance, controls, and stress tests

The 86 pages rulebook explains in detail what is expected of banks in the context of ILAAP. The rulebook gives explicit assessment criteria in order to define what can be expected of banks and supervisory authorities in relation to managing and supervising liquidity risk.

The rulebook comprises of two parts, which addresses the qualitative elements (Part I) and the quantitative elements (Part II) of the ILAAP (see Exhibit I). The qualitative part is based on the publications of the BCBS and the EBA. This part elaborates on such aspects as expectations relating to the strategies, procedures and measures and the liquidity cushions to be maintained by the institution. The quantitative part, which is directly linked to the qualitative part, contains standards for limits, stress tests, maturity calendars, liquidity ratios and monitoring tools.





The other crucial element of ILAAP is that banks must carry out a self-assessment of its liquidity risk management and the related procedures, measures, governance, controls, stress tests etc. In this liquidity self-assessment a Dutch bank thoroughly evaluates its liquidity risk management (processes) and improves them if necessary. The self-assessment allows a bank and the regulator to validate the quality of its liquidity risk management function on a bank wide consolidated level.

The self-assessment is a continuous process which is undertaken in The Netherlands. To comply with ILAAP, a bank is required to submit in-depth information on topics such as the internally required minimum level of liquidity to be maintained, the suitability of the current liquidity profile for the institution and the level of actual liquidity expressed in absolute amounts, applied ratios and limit breaches.

Whenever an institution cannot comply with the requirements of ILAAP, the DNB can enforce the following possible penalties as corrective mechanisms:

- More stringent recurring central bank supervision resulting in an increase of effort required from the respective ALM, Treasury, & Liquidity Risk Management departments,
- Steering on liquidity buffer composition,
- Increase of liquidity buffer requirements,
- Increase of capital requirement

Arguably, the most valuable aspect of ILAAP is that it ensures that a bank reviews its full liquidity risk management function from strategic to operational level, for all 13 ILAAP principles, on a regular basis. In **Exhibit 2**, a generic liquidity risk framework is shown that can be applied over all ILAAP principles:

#### Why liquidity risk management is underrepresented in Basel III

Traditionally, liquidity risk has been underrepresented in the Basel regulation. However, due to the dangerous role played by liquidity dry-ups and spirals in the recent financial crisis (see Brunnermeier (2009) for an extensive overview), the Bank of International Settlements decided to include liquidity risk explicitly in the Basel III framework. Basel III is intended to be fully effective as of 2019. In Europe, Basel 3 will be implemented through the introduction of a Capital Requirements Regulation (CRR) and through changes to the Capital Requirements Directive (CRD IV).

**Exhibit 3** depicts this current Basel III framework along two different themes: firstly it shows regulation in the area of market, credit and operational risk; secondly it shows regulation in the area of liquidity risk.

Along the three columns one can see the three pillars of Basel III: "Minimum capital requirements" (Pillar I), "Supervisory review Process" (Pillar 2) and "Market discipline" (Pillar 3).



**EXHIBIT 2** – Generic liquidity framework used to implement ILAA

Pillar I deals with regulatory capital calculation in which banks must calculate the amount of regulatory capital for the risks they face. Pillar 2 describes the mandatory processes for both banks and regulators to fulfil the capital-adequacy requirements. Banks are required to demonstrate to the regulator that they have an ICAAP procedure in place, in order to assess their economic capital requirement in relation to their risk profile and capital strategy planning. In addition, national regulators are required to review and evaluate banks' ICAAP procedure and risk management processes in the so-called SREP procedure. Pillar 3 aims to encourage market discipline by developing a set of disclosure requirements and additional recommendations.

By examining the two themes of Exhibit I it becomes evident that liquidity risk is currently underrepresented and only managed via the introduction of two liquidity ratios and liquidity monitoring tools in Pillar 1. The treatment of liquidity risk in Pillar 2 is lacking in Europe. In Pillar 2 there are no specific requirements for management of liquidity risk as there are for other type of risks. This differs from the treatment of liquidity risk in Pillars I and 3. Since, under Pillar I, the LCR and NSFR, which are currently being standardised, can be seen as the amount of minimum level of liquidity banks must hold for the liquidity risks they face from a regulatory perspective. Basel III describes specifically how the LCR and NSFR can be calculated and what should be the size of liquid asset buffers. And, currently, Pillar 3 is being standardised with respect to LCR disclosure requirements as this is in the consultation phase.

#### **TopQuants Newsletter**

#### Page 22

Altogether, there is a gap in Pillar 2 between how liquidity risk and credit, market & operational risk is managed and respectively supervised by banks and national regulators. Exhibit 3 reveals that currently this gap is neither solved in ICAAP nor SREP. With regards to ICAAP, the Basel committee does not define capital as a method or practice for banks to attribute capital against liquidity risks they face. In other words, banks do not perform a comprehensive assessment of material liquidity risks by measuring capital. Also, there is not a robust controlling and reporting framework that enables a continuous evaluation of relevant liquidity risk issues. Hence, ICAAP does not result in standard liquidity risk reports for relevant stakeholders and senior management.

Paper scope	<b>Pillar 1</b> Minimum Capital Requirements	<b>Pillar 2</b> Supervisory Review Process	<b>Pillar 3</b> Market discipline
Market, Credit, and Operational Risk	Standardised <ul> <li>Risk Weighted Assets (RWA)</li> <li>Quantity and level of regulatory capital</li> <li>Leverage</li> </ul>	Standardised <ul> <li>ICAAP: capital planning and allocation, limit setting and monitoring</li> <li>SREP: review and evaluation, monitor on-going compliance with standards and identify any weaknesses</li> </ul>	Standardised <ul> <li>Disclosure of capital structure, risk exposure and capital adequacy</li> <li>Market is able to asses capital adequacy</li> <li>Risk reports</li> </ul>
Liquidity Risk	Being standardised • Liquidity Coverage Ratio (LCR) • Net Stable Funding Ratio (NSFR) • Liquidity monitory tools	Not standardised	Being standardised Consultative document issued on LCR and NSFR disclosure standards

**EXHIBIT 3:** Status Basel III pillars per October 2013

#### The Dutch ILAAP ensures a robust liquidity risk management framework.

In order to close the liquidity risk regulatory gap that is present in Basel III Pillar 2, it is recommended to use the Dutch ILAAP (and its rulebook and self-assessment procedure) as baseline. Overall, ILAAP should be considered as complementary to ICAAP and SREP, and not as a substitute. For banks, ILAAP is the solution for managing liquidity risk as ICAAP is for credit risk, market risk, operational risk, business/strategic risk, counterparty credit risk, insurance risk, real estate risk and model risk.

The implementation of Dutch ILAAP has brought a number of key benefits to the Dutch banking system:

- As a first benefit, ILAAP greatly increases consistency between the strategy of the bank (e.g. liquidity risk appetite, funding plan) and operational processes (e.g. collateral management, reporting). The ILAAP liquidity risk management framework is designed to be implemented from a strategic to operational level. A liquidity risk appetite is defined on a strategic level and translated into qualitative statements and risk metrics at an operational level.
- Second, ILAAP makes the expectation of the regulator towards banks in regard of liquidity risk management explicit. Banks know what to expect with regard to liquidity risk management. The liquidity risk principles of the BCBS and the EBA do not go into the same level of detail for all aspects. Therefore, the Dutch regulator opted to introduce ILAAP to answer the question "What is expected of banks and the supervisory authority". The 86 pages of the ILAAP rulebook provide information on the review and evaluation procedures applied for ILAAP and gives explicit assessment and evaluation criteria.
- **Third**, ILAAP gives an overview of the liquidity risks on a bank-wide consolidated level. For example, the ILAAP stress tests allow the institution to analyse the impact of stress scenarios on its consolidated, group-wide, liquidity position and also on its liquidity position of individual entities and business lines.

- Fourth, ILAAP produces a clear publication for the outside world in order to make the liquidity risks of the bank transparent to regulators. For example, the Dutch regulator evaluates ILAAP by looking into the degree to which the institution gives an insight into the role and responsibilities of the relevant committees and the working of the liquidity risk management framework. Also the Dutch regulator evaluates the degree of centralisation or decentralisation of the treasury function and the liquidity risk management function.
- **Fifth,** ILAAP provides a systematic approach to assess liquidity risks and to decide if additional risk controls are required. The bank can execute an internal assessment of how liquidity risk is managed. The internal assessment is a way to check if the required minimum level of liquidity is maintained. Also ILAAP evaluates the suitability of the current liquidity profile of the bank and the level of actual liquidity expressed in absolute amount, ratios and limit breaches, etc.
- **Sixth,** ILAAP initiates an improvement cycle for liquidity risk management within a bank since the Dutch ILAAP self-assessment procedure is a recurring process. A recurring systematic process to assess whether the liquidity risk management function is adequate according to the ILAAP standard on a bank-wide consolidated level.
- Finally, since ILAAP has been implemented since 2011, it has emanated as a proven concept for both Dutch banks and the DNB.

It is foreseen that ILAAP leads to an overall good risk management at banks and ensures a robust liquidity risk management framework

#### Conclusion

This paper identifies a gap in Pillar 2 of the Basel III framework with respect to liquidity risk. This gap can be mitigated by regulation based on BCBS and EBA guidelines and principles. One such regulation is the Dutch ILAAP which is considered to be a viable candidate to fill the Pillar 2 gap, since it well tested in practice and also provides a clear set of rules. A number of benefits have been identified:

Th	e 7 Benefits of Dutch ILAAP	
1.	Consistency	greatly increases consistency between the strategy of the bank (e.g. liquidity risk appetite, funding plan) and operational processes (e.g. collateral management, reporting)
2.	Clear expectations	makes the expectation of the regulator toward banks in regard of liquidity risk management explicit. Banks knows what to expect in regard of liquidity risk management
3.	One comprehensive overview	gives an overview of the liquidity risks on a bank wide consolidated level
4.	Clear reporting requirements	produces a crystal clear publication for the outside world in order to make the liquidity risks of the bank transparent to regulators and investors
5.	Systematic approach	provides a systematic approach to assess liquidity risks and to decide if additional risk controls are required
6.	Improvement cycle	initiates an improvement cycle for liquidity risk management within a bank
7.	Proven concept	the Dutch ILAAP has been in use since 2 years and has grown to a more matured stage

#### **EXHIBIT 4**: The 7 benefits of ILAAP for banks and regulators

There is a critical gap in the Basel 3 framework with respect to liquidity risk under Pillar 2. To mitigate this gap in a timely manner we propose that the Dutch ILAAP should function as a baseline. The European banking system can benefit from these well-tested practices and clear set of rules in a similar manner as the Dutch banks have benefitted from Dutch ILAAP by improving their Liquidity Risk Management.

#### References

[1] Brunnermeier, M., "Deciphering the Liquidity and Credit Crunch 2007-2008", *Journal of Economic Perspectives* 23, 77–100 (2009).

[2] Diamond, D.W., and R.G. Rajan, "Liquidity shortages and banking crisis", Journal of Finance 60, 615-647 (2005).

[3] Van der Wielen, L., Nauta, B., "ALM and Risk. From the Financial Markets' Perspective", ISBN 978-90-816351-9-6 (2013)

#### SPVAs: A Grid GPU Implementation

— by Jeroen Hofman (Front Office Quant, ING)



#### Introduction

Variable annuities are a widely used class of contracts issued mostly by insurers and several big banks. In a typical contract clients invests money in an account and receive (annuitized) returns based on the performance of the account, hence the term variable annuity. Account performance is usually linked to fund groups, which is linked to performance of investment assets, e.g. indices or rates. The contract usually provides several guarantees which protects the clients against poor performance. In this article we focus on a particular set of variable annuity products, namely Single Premium Variable Annuities (SPVAs) with two types of guarantees, where a single initial investment (the single premium) is provided by the client at the start of the contract. In the next section we will introduce a typical SPVA product and describe the liabilities that are attached from the issuers perspective to such a product. For estimation of the liabilities on a large portfolio of SPVA products we motivate the development of a Graphical Processing Unit (GPU) application, capable of computing liabilities for a large number of scenarios. We compare performance between a CPU implementation and a GPU implementation and look at scalability on a grid of GPUs to be able to compute sensitivities (Greeks) on the value of the liabilities with respect to the underlying market parameters.

#### **Single Premium Variable Annuities**

The structure of the product is schematically given in figure 1. An initial premium is paid by the client at the start of the contract (t = 0), which after deduction of fees is invested in an account. The account balance is distributed among a number of fund groups, consisting of collections of bonds and equity indices. During the contract lifetime 0 < t < T the account balance AV(t) changes due to the performance of the underlying funds and guarantees are provided to the client. We consider two types of guarantees:

**MGDB**: Minimum Guaranteed Death Benefit. If the client deceases at time 0 < t < T during the contract period they will receive an amount equal to the greater of the current account balance, the initial single premium or the guarantee level K(t) (see figure 1). Hence we have:

$$MGDB(t) = \max (AV(t), SP, K(t)) - (1)$$

**MGSB**: Minimum Guaranteed Survival Benefit. If the client does not decease or terminate the contract (lapse) prior to T they will receive an amount equal to the greater of the current account balance, the initial single premium or the guarantee level K(T). Hence we have:

$$MGSB(T) = \max (AV(T), SP, K(T)) - (2)$$



Figure I: Schematic overview of an SPVA product.

During the life of the contract, the client can terminate the contract (lapse) in which case it will receive the current account balance. If the contract reaches time T the MGSB guarantee will be triggered and the client has the option of annuitization of the final account balance. Each year the client is active, contract fees are deducted from the account balance to compensate the issuer for the cost of the guarantees, the account management and other costs the issuer might have (e.g. hedging costs).

From the description it is clear that the issuer of these products faces serious risks. There is *mortality risk*, where death of the client triggers the MGDB guarantee. If the current account balance is insufficient to pay the full guarantee, the issuer will have to make additional capital available. Secondly there is *lapse risk*, where at fixed times the client may or may not decide to terminate the contract. Although no guarantee is provided in this situation, the issuer sees its future positive cash-flows reduced (in the form of fees). Coupled to the guarantees there is considerable market risk, as negative markets may lead to poor fund group performance and low account balances, increasing the gap between account balance and guarantee, increasing potential losses for the issuer.

The above paragraph makes it clear that there is a need for calculation of the liabilities, in the form of guarantees, faced by the issuer who is holding a portfolio of SPVA contracts.

#### Model

To measure the liabilities faced by the issuer on a contract we define the present value on the expected liability for the MGSB as:

$$L_{MGSB} = D(T) \max (K(T) - AV(T), 0) IF(T) - (3)$$

where D(T) is the discount factor for time T, K(T) is the guaranteed amount, AV(T) is the account balance and IF(T) is the expected *inforce rate*, the probability that the client has neither lapsed nor deceased up to time T. Note that equation 3 is contract-dependent as mortality rates are dependent on the age of the client and AV(T) is dependent on the initial single premium. Notice that the liability is only depending on quantities at time T, the maturity of the contract.

In a similar way we can define for the MGDB:

 $L_{MGDB} = \Sigma D(t) \max(K(t) - AV(t), 0) Q(t, IF(t - 1)) - (4)$ 

where the summation is taken over all times  $0 \le t \le T$ . We consider the entire maturity of the contract 0 < t < T as the death benefit can be triggered at any time by death of the client. Q(t, IF(t - 1)) is the expected mortality rate between t and t + 1, depending on the age of the client and the current inforce rate IF(t), i.e. the probability that the client has neither lapsed nor deceased prior to t.

To calculate the liabilities we need the following data:

• Q(t): The mortality rates based on the age of the client. We use mortality tables provided by the statistics bureau of the country in which the contracts are issued.

• AV(t): The account balance at future time t based on fund group performance. We describe the account value projection briefly in the following section.

• K(t): The guarantee depends on the initial premium, given in the contract, and the history up to time t of the account value. If the account value reaches a certain threshold the guarantee 'locks in' at that level, see figure 1.

• IF(t): This variable incorporates information from both Q(t, IF(t - 1)) and the lapse rate L(t, K(t)/AV(t)) where the rates are empirically estimated based on time t and moneyness K(t)/AV(t).

Using standard Monte-Carlo techniques we can generate scenarios consisting of simulations of the risk-factors underlying the account value (see below). A reliable estimate of the liabilities can be computed by averaging the liability as defined in equations 3 and 4 over all scenarios.

#### **Account Value Process**

We can simulate the account value process in the future by simulating the underlying fund groups. Fund groups can consist of both domestic and foreign equity indices and domestic and foreign bond funds. To model the fund group process we model the underlying riskfactors as a hybrid Hull-White Black-Scholes model with time-dependent volatility, where we use discretized processes for the short rates of all the currencies involved, the exchange rates from foreign currencies to the domestic currency and the equity indices.

Using this hybrid model we model fund groups and bond indices as a basket of underlying risk-factors, e.g. we can have a fund group with a historical composition of 30% of investments in the EURSTOXX50 index, 30% in the S&P 500 and 40% of investments in USD treasury bonds. The fund group projection together with fee data (specified in the contract) and investment allocation among fund groups (also specified in the contract), allows us to model the account value and hence also the guarantee K(t) and inforce rate IF(t).

#### **GPU** Implementation

We are interested in computing the Monte-Carlo average of the liabilities as described in the previous section. To do so we need to do the following:

• Compute scenarios for the riskfactors as described above. We need typically around 200,000 scenarios for the liabilities to have a Monte Carlo error of less than 1%.

• Compute account value processes and liabilities for each contract separately, as the initial premium, fees, age and lapse assumptions are different per contract. A portfolio can easily consist of a number of contracts in the order of  $10^5$ .

· Ideally we would like to revalue the liabilities of the contracts by bumping market data to obtain sensitivities. Since

fund groups consist of baskets of risk-factors the number of revaluations are typically in the order of 10<sup>2</sup>.

Given the massive size of this problem, considering a GPGPU for doing (part of) the calculation is a natural step. GPUs are nowadays widely used in finance and have proven to perform in the area of option pricing and pricing applications like CVA [1], and applications for products similar to SPVAs exist [2][3].

One of the key components of proper use of the compute capabilities of a GPU is memory management. In the implementation that was built features like *shared memory* and *constant memory*, as well as optimization of *memory coalescence* and minimization of *warp divergence* were taken into account, the interested reader can have a look at [5]. A large amount of time was invested to optimize the calculations on the GPU as much as possible, as achieving good performance is non-trivial for an application of this scale.

#### Results

To measure the performance of the GPU implementation we bench-marked it against a C++ implementation, calculating on a single CPU. We computed the liabilities averaged over 5,000 Monte-Carlo scenarios for a portfolio of 400,000 SPVA contracts. The results are given in table 1.

Model Component	CPU	GPU	Speedup	
Data Reading	13.09	14.53	0.90	
Scenario Generation	16.35	0.89	18.38	
(Risk-factors + Fund groups)				
Liability Calculation	107,738	778	138.10	
Total	107,767	793	135.45	

Table I: Execution time (s) per component.

We see a large speedup for the liability calculation (which includes account value projection) of approximately a factor of 138. As the liability calculation is the bottleneck for performance we have greatly reduced the total execution time of the program to 13 minutes for 5,000 scenarios. Furthermore, we can scale up on a grid of GPUs with an efficiency greater then 90%, as is shown by figure 2.





The computation time we achieved by using a GPU allows us to do intra-day valuations of a SPVA portfolio, as well as computing Greeks and other sensitivities on the portfolio by using standardized bump-and-revalue techniques, reducing the average computation time for Greek calculations back from a scale of days to a scale of hours or minutes.

#### Acknowledgments

I would like to thank David Schrager and Andy Sklodowski from their support from the SPVA trading desk, furthermore I would like to thank my colleagues Drona Kandhai, Vladislav Sergeev and Tim Wood for their input for my graduation thesis, where this article is based upon.

#### References

[1] V. Savickas et al., Super Fast Greeks: An Application to Counterparty Valuation Adjustments, Wilmott magazine, Vol. 2014, No. 69, 76-81, 2014.

[2] D. Bogg, Standard Life Canada adopts Aon Benfield's PathWise TM platform, April 27, 2011, source: http://aon.mediaroom.com/index.php?s=25776&item=64210

[3] People Like VAs Like GPUs, Wilmott magazine, Vol. 2012, No. 60, 10-13, 2012.

[4] Algorithm of prefix sum scan using CUDA, <u>http://http.developer.nvidia.com/GPUGems3/gpugems3\_ch39.html</u>

[5] CUDA Toolkit Documentation, http://docs.nvidia.com/cuda/

#### **Upcoming Events**

1. The next event is the 2014 TopQuants Spring workshop on May 28th. The event will be hosted by De Nederlandsche Bank (DNB). The official invitation will be mailed soon and further details of the event will be posted in due course on the TopQuants homepage.

2. The next issue of the TopQuants newsletter will follow in September 2014. Contributions for it are already welcome. Kindly contact Aneesh Venkatraman, (newsletter@topquants.nl).